## AQA Maths M2

# Topic Questions from Papers <br> Energy, Work and Power 

Answers

\begin{tabular}{|c|c|c|c|c|}
\hline \begin{tabular}{l}
1 (a) \\
(b)(i) \\
(ii)
\end{tabular} \& \[
\begin{aligned}
P \& =(30 \times 42) \times 42 \\
\& =52920 \mathrm{~W}
\end{aligned}
\]
\[
F=1200 \times 9.8 \sin 5^{\circ}+30 v
\]
\[
\begin{aligned}
\& 52920=\left(1200 \times 9.8 \sin 5^{\circ}+30 v\right) v \\
\& v^{2}+392 \sin 5^{\circ} v-1764=0
\end{aligned}
\]
\[
\begin{aligned}
\& v=\frac{-392 \sin 5^{\circ} \pm \sqrt{\left(392 \sin 5^{\circ}\right)^{2}-4 \times 1 \times(-1764)}}{2 \times 1} \\
\& v=28.3 \text { or }-62.4 \\
\& \mathrm{v}=28.3 \mathrm{~ms}^{-1}
\end{aligned}
\] \& \begin{tabular}{l}
M1 \\
A1 \\
M1A1 \\
dM1 \\
A1 \\
M1
\end{tabular} \& 2

4

4 \& | Finding force |
| :--- |
| Correct answer from $P=F v$ |
| Finding force. Correct force |
| Using $P=F v$ |
| Correct equation from correct working AG |
| Solving quadratic |
| Correct solution | <br>

\hline \& Total \& \& 8 \& <br>
\hline
\end{tabular}

(Q4, Jan 2006)

| 2 (a) | $\begin{aligned} & \frac{100}{0.4} e=10 \times 9.8 \\ & e=0.392 \mathrm{~m} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 | Use of Hookes law and equilibrium Correct length |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $\begin{aligned} & E P E=\frac{1}{2} \times \frac{100}{0.4} \times 0.6^{2}=45 \mathrm{~J} \\ & \mathrm{AG} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 2 | Use of EPE formula Correct value from correct working |
| (c)(i) | $45=\frac{1}{2} \times \frac{100}{0.4}(x-0.4)^{2}+\frac{1}{2} \times 10 v^{2}+10 \times 9.8(1-x)$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \end{aligned}$ |  | Expression for EPE with $(x \pm 0.4)^{2}$ <br> Correct EPE <br> Four term energy equation |
|  | $45=125(x-0.4)^{2}+5 v^{2}+98(1-x)$ | $\begin{aligned} & \mathrm{B} 1 \\ & \mathrm{~A} 1 \end{aligned}$ |  | Correct GPE <br> Correct equation |
|  | $5 v^{2}=98 x-98+45-125 x^{2}+100 x-20$ | dM1 |  | Solving for $v^{2}$ |
|  | $v^{2}=39.6 x-25 x^{2}-14.6 \mathrm{AG}$ | A1 | 7 | Correct result from correct working |
| (ii) | $39.6 x-25 x^{2}-14.6=0$ |  |  |  |
|  | $25 x^{2}-39.6 x+14.6=0$ |  |  |  |
|  | $x=\frac{39.6 \pm \sqrt{39.6^{2}-4 \times 25 \times 14.6}}{\text { 信 }}$ | M1 |  | Solving quadratic |
|  | $x=\frac{2 \times 25}{}$ |  |  |  |
|  | $=1$ or 0.584 | A1 |  | Correct solutions |
|  | $x=0.584$ | A1 | 3 | Appropriate value selected SC Only correct answers given, award M1A1. |
|  | Total |  | 14 |  |


| 3 (a) | $\mathrm{EPE}=\frac{1}{2} \times \frac{30}{0.5} \times 1.3^{2}=50.7 \mathrm{~J}$ | $\begin{aligned} & \mathrm{M} 1 \\ & \text { A1 } \end{aligned}$ | 2 | use of EPE formula correct EPE |
| :---: | :---: | :---: | :---: | :---: |
| (b)(i) | $\begin{align*} & 50.7=\frac{1}{2} \times 2 v^{2}+\frac{1}{2} \times \frac{30}{0.5} \times 0.8^{2} \\ & 50.7=v^{2}+19.2  \tag{AG}\\ & v=\sqrt{31.5}=5.61 \mathrm{~ms}^{-1} \end{align*}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { A1 } \\ \text { dM1 } \\ \text { A1 } \end{gathered}$ | 5 | three term energy equation two terms correct all terms correct solving for $v$ correct $v$ from correct working |
| (ii) | $\begin{aligned} & 50.7=\frac{1}{2} \times 2 v^{2} \\ & v=\sqrt{50.7}=7.12 \mathrm{~ms}^{-1} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | 3 | two term energy equation correct equation <br> correct velocity |
| (c) | $\frac{1}{2} \times 2 v^{2}=50.7-1.8 \times 0.1 \times 2 \times 9.8$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ |  | finding friction force correct friction force three term energy equation correct equation |
|  | $v=\sqrt{47.172}=6.87 \mathrm{~ms}^{-1}$ | A1 | 5 | correct velocity |
|  | Total |  | 15 |  |

(Q3, June 2006)

\begin{tabular}{|c|c|c|c|c|}
\hline \begin{tabular}{l}
4 (a) \\
(b) \\
(c)
\end{tabular} \& \begin{tabular}{l}
\[
\begin{aligned}
\& \frac{1}{2} \times 35 \times v^{2}=35 \times 9.8 \times 10 \\
\& v=14\left(\mathrm{~ms}^{-1}\right)
\end{aligned}
\] \\
Air resistance or friction \\
Energy lost =
\[
35 \times 9.8 \times 10-\frac{1}{2} \times 35 \times 12^{2} \quad(=910)
\] \\
Work done: \(F \times 20 \quad(=910)\) \\
\(20 F=910\) \\
\(F=45.5(\mathrm{~N})\)
\end{tabular} \& \begin{tabular}{l}
M1 \\
A1 \\
A1 \\
B1 \\
M1 \\
A1 \\
m1 \\
A1
\end{tabular} \& 3
1

4 \& | Energy method |
| :--- |
| Difference attempted $\pm$ $F>0$ | <br>

\hline \& Total \& \& 8 \& <br>
\hline
\end{tabular}

(Q1, Jan 2007)


| 6 (a) | $\begin{aligned} \text { Kinetic energy } & =\frac{1}{2} \times 5 \times 10^{2} \\ & =250 \mathrm{~J} \end{aligned}$ | M1 <br> A1 | 2 | Full method |
| :---: | :---: | :---: | :---: | :---: |
| (b) | Using conservation of energy: <br> KE when box hits ground <br> $=$ Initial $\mathrm{KE}+$ Change in potential energy $=250+5 \times 30 \times g$ $=1720 \mathrm{~J}$ | M1 <br> A1ft <br> A1 | 3 | Could have sign errors $\text { AG; SC2 } 5 \times 35.1 \times g=1720 . \ldots$ |
| (c) | $\begin{aligned} & \frac{1}{2} m V^{2}=1720 \\ & V^{2}=688 \\ & \therefore \text { Speed is } 26.2 \mathrm{~m} \mathrm{~s}^{-1} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | 3 | CAO; accept $\sqrt{688}$ or $4 \sqrt{43}$; SC2 26.3 |
| (d) | No air resistance Box is a particle | $\begin{aligned} & \text { E1 } \\ & \text { E1 } \end{aligned}$ | 2 | Or no resistance forces Deduct 1 mark for unacceptable third reason |
|  | Total |  | 10 |  |


(Q6, June 2007)

| 8 (a) | $\begin{aligned} \text { Kinetic energy } & =\frac{1}{2} \times 0.6 \times 15^{2} \\ & =67.5 \mathrm{~J} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 |  |
| :---: | :---: | :---: | :---: | :---: |
| (b) | Using $m g h=\frac{1}{2} m v^{2}$ : | M1 |  |  |
|  | $\begin{aligned} 67.5 & =0.6 \times g \times h \\ \Rightarrow h & =\frac{67.5}{0.6 g} \\ & =11.5 \mathrm{~m} \end{aligned}$ | A1 A1 | 3 |  |
| (c) | When 3 m above ground level: Change in PE is $0.6 \times g \times 3$ $=17.64 \mathrm{~J}$ |  |  |  |
|  | $\begin{aligned} & \therefore \mathrm{KE} \text { of ball is } 67.5-17.64 \\ & =49.86 \mathrm{~J} \end{aligned}$ | M1 A1 |  |  |
|  | Speed of ball is $\sqrt{\frac{49.86}{\frac{1}{2} \times 0.6}}$ | m1 |  | Dep on M1 |
|  | $=12.9 \mathrm{~m} \mathrm{~s}^{-1}$ | A1 | 4 | No KE given: speed $=12.9$ SC3 |
| (d) | eg ball is a particle, no air resistance, weight is the only force acting etc | E1 | 1 | Accept no spin, no wind |
|  | Total |  | 10 |  |

\begin{tabular}{|c|c|c|c|c|}
\hline \begin{tabular}{l}
9 (a) \\
(b) \\
(c)
\end{tabular} \& \begin{tabular}{l}
\[
\begin{aligned}
\& \mathrm{EPE}=\frac{\lambda x^{2}}{2 l} \\
\& =\frac{300 \times(1.5)^{2}}{2 \times 4} \\
\& =84.375 \\
\& =84.4 \mathrm{~J}
\end{aligned}
\] \\
When string is slack, gain in PE is \(m g h\)
\[
\begin{aligned}
\& =6 \times g \times 1.5 \sin 30 \\
\& =44.1 \mathrm{~J} \\
\& \mathrm{KE}=\mathrm{EPE}-\text { gain in } \mathrm{PE} \\
\& =84.375-44.1 \\
\& =40.275 \\
\& \frac{1}{2} .6 . v^{2}=40.275 \\
\& v=3.66
\end{aligned}
\] \\
At \(A\), PE gained above initial position is
\[
\begin{aligned}
\& 6 \times g \times 5.5 \sin 30 \\
\& =161.7 \mathrm{~J}
\end{aligned}
\] \\
This is more than initial elastic potential energy \\
\(\therefore\) particle will not reach \(A\)
\end{tabular} \& \begin{tabular}{l}
M1 \\
A1 \\
M1 \\
A1 \\
m1 \\
A1 \\
A1 \\
B1 \\
B1 \\
E1
\end{tabular} \& 2

5

3 \& | AG |
| :--- |
| Or PE above position string slack is 117.6 KE at $A$ is -77.3 |
| Or |
| Using $v^{2}=u^{2}+2 a s$ |
| $a=0.5 g \quad$ B1 |
| $s=1.37$ or $1.366 \quad$ B 1 [or 2.87 above starting point] |
| Hence stops before $A$ E1 |
| Vertical height above sling slack is 0.683 |
| Vertical height above starting point is | <br>

\hline \& Total \& \& 10 \& <br>
\hline
\end{tabular}

(Q6, Jan 2008)

\begin{tabular}{|c|c|c|c|c|}
\hline \begin{tabular}{l}
10 (a) \\
(b)
\end{tabular} \& \begin{tabular}{l}
\[
\begin{aligned}
\& \text { Using power }=\text { force } \times \text { velocity } \\
\& \text { Power }=(40 \times 50) \times 50 \\
\& \therefore=100,000 \text { watts }
\end{aligned}
\] \\
When speed is 25 , max force exerted is \(\frac{100000}{25}\) \(=4000 \mathrm{~N}\) \\
\(\therefore\) Accelerating force is 3000 N \\
Using \(F=m a\)
\[
3000=1500 a
\]
\end{tabular} \& \begin{tabular}{l}
M1 \\
A1 \\
B1 \\
M1
\end{tabular} \& 2 \& \[
\begin{aligned}
\& \text { Need } 3 \text { terms eg } ‘ 4000 ’ \pm 1000=m a \\
\& \text { or } 2000 \pm 1000=m a \\
\& \text { M0 for } 1000=m a
\end{aligned}
\] \\
\hline (c) \& \begin{tabular}{l}
\[
a=2 \mathrm{~ms}^{-2}
\] \\
When van is at maximum speed force against gravity is \(m g \sin 6\) (parallel to slope) \\
Force against gravity and resistance is
\[
\begin{aligned}
\& m g \sin 6+40 v \\
\& \quad=1536.6+40 v
\end{aligned}
\] \\
Speed is maximum
\[
\text { when } 1536.6+40 v=\frac{100000}{v}
\]
\[
40 v^{2}+1536.6 v-100000=0
\] \\
Speed is \(34.4 \mathrm{~ms}^{-1}\)
\end{tabular} \& \begin{tabular}{l}
A1 \\
B1 \\
M1 \\
A1 \\
M1 \\
A1 \\
A1
\end{tabular} \& 3

6 \& For 3 terms; $\frac{100000}{v}$ and 1 other term correct CAO <br>
\hline \& Total \& \& 11 \& <br>
\hline
\end{tabular}

11 (a)

Work done $=\int_{0}^{e} \frac{\lambda x}{l} \mathrm{~d} x$
$=\left[\frac{\lambda x^{2}}{2 l}\right]_{0}^{e}$
$=\frac{\lambda e^{2}}{2 l}$
Or
Area under a straight line $=$
average force $\times$ distance $=\frac{\lambda e^{2}}{2 l}$
(b)(i)

Using $T=\frac{\lambda x}{l}$

$$
5 g=\frac{150 \times x}{0.6}
$$

Extension is 0.196 m
(ii)
$\mathrm{EPE}=\frac{\lambda x^{2}}{2 l}$

$$
=\frac{150 \times(0.3)^{2}}{2 \times 0.6}
$$

$$
=11.25 \mathrm{~J}
$$

(iii) When $x$ above $P$,
$\mathrm{EPE}=\frac{150 \times(0.3-x)^{2}}{2 \times 0.6}$
$\mathrm{PE}[$ relative to $P]=(-) 5 \times g \times x$
KE + EPE [at new point]
$=$ EPE [at $P]$ - gain in PE
$\frac{1}{2} m v^{2}+\frac{150 \times(0.3-x)^{2}}{2 \times 0.6}=$

$$
\frac{150 \times(0.3)^{2}}{2 \times 0.6}-5 g x
$$

$\frac{1}{2} m v^{2}+\frac{150 \times\left(x^{2}-0.6 x\right)}{2 \times 0.6}=-5 g x$
$\frac{1}{2} .5 \cdot v^{2}+125 x^{2}-75 x=-49 x$
$v^{2}=10.4 x-50 x^{2}$
(iv)

Particle is at rest when $v=0$
$10.4 x-50 x^{2}=0$
$x=0$ [not required]
Or $x=\frac{10.4}{50}=0.208 \mathrm{~m}$ above $P$.

Needs limit of 0

AG

2
A1

M1
A1
2
for $\frac{150 \times(\ldots-x)^{2}}{2 \times 0.6}$
for $5 \times g \times$ distance

4 terms, all signs correct, 2 terms correct

Equation involving terms in $v^{2}, x^{2}$ and $x$ only

| 12 (a) | $\begin{aligned} \text { Initial } \begin{aligned} \mathrm{KE} & =\frac{1}{2} m v^{2} \\ & =\frac{1}{2} \times 6 \times 12^{2} \\ & =432 \mathrm{~J} \end{aligned},=\text {. } \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 | Allow one of $m$ and $v$ incorrect |
| :---: | :---: | :---: | :---: | :---: |
| (b)(i) | When it hits the ground, conservation of energy gives $\begin{aligned} \mathrm{KE} & =\text { Initial } \mathrm{KE}+\text { loss in } \mathrm{PE} \\ & =432+6 \times g \times 4 \\ & =667.2 \\ & =667 \mathrm{~J}(3 \mathrm{sf}) \end{aligned}$ | M1 A1 | 2 | Need $6 \times g \times 4$ or 235.2 AG |
| (ii) | $667.2=\frac{1}{2} \times 6 \times v^{2}$ <br> Speed is $14.9 \mathrm{~m} \mathrm{~s}^{-1}$ | M1A1 A1 | 3 |  |
| (iii) | Stone is a particle <br> No air resistance | $\begin{aligned} & \mathrm{B} 1 \\ & \text { B1 } \\ & \hline \end{aligned}$ | 2 | Not $g$ constant No other forces acting |
|  | Total |  | 9 |  |

(Q2, Jan 2009)

| $13 \text { (a) }$ <br> (b) | At maximum speed, tractive force $=$ resistance force Using power $=$ force $\times$ velocity: $800000=F \times 40$ $\mathrm{F}=20000 \mathrm{~N}$ <br> Using force $\times$ distance $=$ work done $=$ change in energy: $20000 s=\frac{1}{2} \times 60000 \times\left(40^{2}-36^{2}\right)$ $\text { Distance }=456 \mathrm{~m}$ | M1 <br> M1 <br> A1 <br> M1 <br> A1 <br> A1 <br> A1 | 3 | M1 Fs = change of KE A1 2 of 3 terms correct A1 all 3 terms correct |
| :---: | :---: | :---: | :---: | :---: |
|  | Total |  | 7 |  |


(Q9, Jan 2009)

15 (a)

(b) Change in PE as slides down:
$m g h=55 \times 9.8 \times 20 \cos 30$

$$
=9335.7 \ldots
$$

Using Conservation of Energy:
KE at end of slide $=247.5+9335.7$
Speed of Anne is $\sqrt{\frac{9580 \mathrm{~J}}{\frac{9583}{\frac{1}{2} \times 55}}}$

$$
=18.7 \mathrm{~m} \mathrm{~s}^{-1}
$$

(c)

Anne is a particle; no air resistance

|  | M1 |  |  |
| :--- | :---: | :---: | :--- |
|  | A1 | 2 |  |
|  | M1 |  | Need $\cos 30$ or $\sin 30$ |
| A1 |  |  |  |
|  | m1 |  | 'a' +9335.7 <br> accept 9583 |
|  | A1 |  |  |
|  | m1 |  |  |
|  | A1 | 6 |  |
| Total |  | 9 |  |


| 16 | Force acting against gravity is $m g \sin \theta$ <br> Force acting against gravity and resistance is $m g \sin \theta+200000$ $\begin{aligned} & =600000 g \sin \theta+200000 \\ & =347000 \end{aligned}$ $\begin{aligned} \text { Using power } & =\text { force } \times \text { velocity } \\ & =347000 \times 24 \\ & =8330 \mathrm{~kW} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { m1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1F } \\ \text { A1 } \end{gathered}$ | 6 | Or 147000 $200000+{ }^{\prime} \mathrm{mg} \sin \theta^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | Total |  | 6 |  |

(Q5, June 2009)

| 17 (a) | $\begin{aligned} \text { EPE } & =\frac{\lambda x^{2}}{2 l} \\ & =\frac{180 \times 0.8^{2}}{2 \times 1.2} \\ & =48 \mathrm{~J} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 |  |
| :---: | :---: | :---: | :---: | :---: |
| (b) | Using initial $\mathrm{EPE}=\mathrm{KE}$ when string becomes slack: $\begin{aligned} 48 & =\frac{1}{2} \times 5 \times v^{2} \\ v & =\sqrt{\frac{96}{5}} \\ & =4.38 \mathrm{~m} \mathrm{~s}^{-1} \end{aligned}$ | M1 <br> A1F <br> A1F | 3 | $\mathrm{ft} \sqrt{\frac{\mathrm{a}^{\prime}}{2.5}}$ |
| (c) | Normal reaction is $5 g$ or 49 <br> Frictional force is $5 g \times \mu$ <br> Work done by frictional force is $5 \mu g \times 2$ $=10 \mu g$ <br> Stops at wall $\Rightarrow 10 \mu g=48$ $\mu=0.490$ | $\begin{gathered} \text { M1 } \\ \text { m1A1 } \\ \text { m1 } \\ \text { A1 } \\ \text { m1 } \\ \text { A1 } \end{gathered}$ | 7 | $\begin{aligned} & \mathrm{m} 110 \mu g=' a ' \\ & \text { accept } \frac{24}{49} \text { OE } \end{aligned}$ |
|  | Total |  | 12 |  |

(Q6, June 2009)

| 18 | Work done $=F s \cos \theta$  <br>  $=40 \times 5 \times \cos 30$ <br> $=173 \mathrm{~J}$  | M1 |  | Accept Fs $\sin \theta$ for M1 |
| :--- | :--- | :---: | :---: | :---: |
|  |  | A1 |  |  |
|  | Total |  | 3 |  |

(Q1, Jan 2010)

| 19 (a) | When $x \geq 22$, KE is $\frac{1}{2} \times 49 \times v^{2}$ <br> EPE is $\frac{1078(x-22)^{2}}{2 \times 22}$ <br> Change in PE is $49 \times g \times x$ <br> Conservation of energy: $\begin{aligned} & \frac{1}{2} \times 49 \times v^{2}+\frac{1078(x-22)^{2}}{2 \times 22}=49 \times g \times x \\ & \frac{49}{2} v^{2}+\frac{49}{2}(x-22)^{2}=49 g x \\ & v^{2}+(x-22)^{2}=19.6 x \end{aligned}$ | M1A1 $\begin{gathered} \text { M1A1 } \\ \text { A1 } \end{gathered}$ |  | M1 for any $\frac{1078 p^{2}}{2 \times 22}$ <br> M1 3 terms (KE, PE, EPE) <br> A1 2 terms correct <br> A1 all 3 terms correct <br> $\mathrm{SC} 3 \frac{49}{2} v^{2}+\frac{49}{2} \mathrm{e}^{2}=49 g(\mathrm{e}+22)$ <br> [could use $x$ for e] |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $5 v^{2}=318 x-5 x^{2}-2420$ <br> If $x$ is not greater than 22 , cord is not stretched | A1 <br> B1 | 6 1 | AG |
| (c) | At maximum value of $x, v=0$ $\begin{aligned} & \therefore 5 x^{2}-318 x+2420=0 \\ & x=\frac{318 \pm \sqrt{318^{2}-4 \times 5 \times 2420}}{2 \times 5} \\ & x=54.76 . . \text { or } 8.84 . . \\ &=54.8 \end{aligned}$ | M1 <br> m1 <br> A1 <br> E1 | 4 | dep on M1 above <br> A1 for either solution <br> Needs to give a reason for deletion of second root. Both roots must be positive: one above 22 , one below 22 |
| (d)(i) | When speed is a maximum, $a=0$ tension $=$ gravitational force | M1 |  | $\begin{aligned} & \text { or } \\ & \frac{\mathrm{d}\left(5 v^{2}\right)}{\mathrm{d} x}=318-10 x \end{aligned}$ |
|  | $\begin{aligned} & \frac{1078(x-22)}{22}=49 g \\ & x-22=9.8 \\ & x=31.8 \end{aligned}$ | A1 A1 | 3 | $=0$ at maximum speed $\Rightarrow 318-10 x=0$ AG |
| (ii) | From part (a), $v^{2}=19.6 \times 31.8-9.8^{2}$ $v=22.96$ <br> Maximum speed is $23.0 \mathrm{~ms}^{-1}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 |  |
|  | Total |  | 16 |  |

(Q8, Jan 2010)

(Q2, June 2010)

| 21 (a) | $\begin{aligned} & \text { Using power }=\text { force } \times \text { velocity } \\ & \begin{aligned} \text { Power } & =(30 \times 48) \times 48 \\ & =69120 \mathrm{watts} \end{aligned} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 2 | AG |
| :---: | :---: | :---: | :---: | :---: |
| (b) | When speed is $40 \mathrm{~m} \mathrm{~s}^{-1}$, max force exerted is $\frac{69120}{40}$ |  |  |  |
|  | $=1728 \mathrm{~N}$ | B1 |  |  |
|  | Accelerating force is ' 1728 ' -1200 N Using $F=m a$ : | M1 |  |  |
|  | $\begin{aligned} & 528=1200 a \\ & a=0.44 \mathrm{~m} \mathrm{~s}^{-2} \end{aligned}$ | $\begin{aligned} & \text { m1 } \\ & \text { A1 } \end{aligned}$ | 4 |  |
| (c) | Force exerted by engine is $\frac{69120}{v}$ | B1 |  |  |
|  | Force exerted by the engine $=30 v-m g \sin 3$ | M1 |  | (Use of $\cos 3$ delete $\mathrm{A} 1, \mathrm{~A} 1$ of 3 A terms) |
|  | $30 v-615.47(\text { or } 1200 g \sin 3)=\frac{69120}{v}$ | A1A1 |  | A2 All terms correct <br> A1 Two terms correct |
|  | $30 v^{2}-615.47 v-69120=0$ | A1 |  | SC3 for $30 v^{2}+615.47 v-69120=0$ |
|  | $v=\frac{615.47 \pm \sqrt{615.47^{2}+4 \times 30 \times 69120}}{2 \times 30}$ | M1 |  |  |
|  | Speed is $59.3 \mathrm{~m} \mathrm{~s}^{-1}$ | A1 | 7 |  |
|  | Total |  | 13 |  |

(Q6, June 2010)

| 22 (a) | PE lost is <br> $=4 \times g \times 5 \cos 70$ <br> $=67.0 \mathrm{~J}$ | M 1 A 1 | 2 | $\mathrm{M} 14 \times g \times 5 \times \cos$ or $\sin 20$ or 70 |
| ---: | :--- | :---: | :---: | :--- |
| (b) | KE is loss of $\mathrm{PE} \Rightarrow \mathrm{KE}$ is 67.0 J |  |  |  |
| (c) | B 1 | 1 | ft |  |
| Using $\mathrm{KE}=\frac{1}{2} m v^{2}$ |  |  |  |  |
| $v^{2}=33.5$ |  |  |  |  |
| Speed of particle is $5.79 \mathrm{~m} \mathrm{~s}^{-1}$ | M 1 |  |  |  |
|  |  | A 1 | 2 | (ft from (b)) |

(Q2, Jan 2011)

(Q3, Jan 2011)


| $25 \text { (a) }$ <br> (b) | $\begin{aligned} \mathrm{KE} & =\frac{1}{2} \times 58 \times 2^{2} \\ & =116 \mathrm{~J} \end{aligned}$ <br> Change in PE: $m g h=58 \times 9.8 \times 7$ $=3978.8$ $\begin{aligned} \mathrm{KE} & =3978.8+116 \mathrm{~J} \\ & =4094.8 \mathrm{~J} \end{aligned}$ <br> Speed of Kim is $\sqrt{\frac{4094.8}{\frac{1}{2} \times 58}}$ $\begin{aligned} & =11.88 \mathrm{~m} \mathrm{~s}^{-1} \\ & =11.9 \mathrm{~m} \mathrm{~s}^{-1} \end{aligned}$ | M1 <br> A1 <br> M1 <br> A1 <br> M1 <br> dM1 <br> A1 | 2 | M1: Correct fully substituted expression for KE. <br> A1: CAO <br> M1: Expression for PE with 58 and 9.8 or 9.81 with 6 or 7 for the height (or 11 and 4,11 and 5 or 10 and 4 ). <br> A1: Accept 3980 or 3970 or 3978 or 3979 or 3978.8. <br> Accept 3982 or 3983 or 3980. <br> M1: Adding their two previous answers. <br> dM 1 : Seeing expression for $v\left(\operatorname{not} v^{2}\right)$, dependent on second M1 <br> A1: Accept 11.88 or 11.8 or 11.9 Accept 11.88 or 11.8 or 11.9 or AWRT 11.89 from $g=9.81$. <br> Obtaining $v=\sqrt{u^{2}+2 g h}$ followed by incorrect substitution M0M1M1, unless $h$ is 6 or 7, which is M1M1M1 <br> 11.0 (from $h=6$ ) M1M1M1 $\begin{array}{rlrl} v & =\sqrt{2^{2}+2 \times g \times 7} & \text { M1M1M1 } \\ & =\sqrt{141.2} & \mathrm{~A} 1 \\ & =11.9 & & \mathrm{~A} 1 \\ & & \\ & =\sqrt{4+14 g} & & \text { M1M1M1A1 } \\ & =11.9 & \text { A1 } \\ v & =\sqrt{2^{2}+12 g} & & \text { M1M1M1 } \end{array}$ |
| :---: | :---: | :---: | :---: | :---: |
|  | Total |  | 7 |  |

(Q1, June 2011)

| $26 \text { (a) }$ <br> (b) | $\begin{aligned} 90 \mathrm{~km} \mathrm{~h}^{-1} & =90 \times \frac{1000}{3600} \mathrm{~m} \mathrm{~s}^{-1} \\ & =25 \mathrm{~m} \mathrm{~s}^{-1} \end{aligned}$ $\begin{aligned} & \text { Resistance is } 5000 \mathrm{~N} \\ & \begin{aligned} \text { Using power } & =\text { force } \times \text { velocity } \\ & =5000 \times 25 \\ & =125 \mathrm{~kW} \end{aligned} \end{aligned}$ | B1 <br> B1 <br> M1 <br> A1 | 3 | B1: Must see $\frac{1000}{3600}$ or $\frac{1000}{60^{2}}$. <br> B1: Obtaining 5000 . <br> M1: Using $P=F v$ with 25 and their $F$. <br> A1: Correct final answer, must be in kW . <br> 125 W or 125000 W B1M1 <br> 125 B1M1A1 |
| :---: | :---: | :---: | :---: | :---: |
|  | Total |  | 4 |  |


(Q9, June 2011)

(Q1, Jan 2012)

\begin{tabular}{|c|c|c|c|c|}
\hline \begin{tabular}{l}
\[
29 \text { (a) }
\] \\
(b)
\end{tabular} \& \begin{tabular}{l}
using power \(=\) force \(\times\) velocity \\
power \(=(25 \times 42) \times 42\) \\
\(\therefore\) power is 44100 watts \\
when speed is \(15 \mathrm{~m} \mathrm{~s}^{-1}\), max force exerted is \(\frac{44100}{15}\)
\[
=2940 \mathrm{~N}
\] \\
resistance force is \(25 \times 15=375 \mathrm{~N}\) \\
accelerating force is \(2940-375 \mathrm{~N}\)
\[
=2565
\] \\
using \(F=m a\)
\[
2565=1500 a
\]
\[
a=1.71 \mathrm{~m} \mathrm{~s}^{-2}
\]
\end{tabular} \& \begin{tabular}{l}
M1 \\
A1 \\
B1 \\
M1 \\
m1 \\
A1
\end{tabular} \& 2

4 \& <br>
\hline \& Total \& \& 6 \& <br>
\hline
\end{tabular}

(Q4, Jan 2012)

| 30 (a) | $\begin{aligned} & \text { using } \mathrm{EPE}=\frac{\lambda x^{2}}{2 l} \\ & \mathrm{EPE}=\frac{32 \times 2.2^{2}}{2 \times 0.8} \\ & =96.8 \mathrm{~J} \end{aligned}$ | M1 <br> B1 <br> A1 | 3 | B1 for 2.2 |
| :---: | :---: | :---: | :---: | :---: |
| (b) | by C of Energy, when next at rest, EPE (initial) = work done against friction + EPE (when at rest) $32 \times 1.2^{2}$ | M1A1 |  | M1A1 for work done by friction or $5 F$ |
|  | $96.8=F \times 5+\frac{3 \angle \times 1.2}{2 \times 0.8}$ | M1A1 |  | M1 3 terms; A1 all correct |
|  | $5 F=96.8-28.8$ <br> frictional force is 13.6 N | $\begin{aligned} & \text { B1 } \\ & \text { A1 } \end{aligned}$ | 6 | B1 28.8 |
| (c) | at B , tension is $\frac{32 \times 1.2}{0.8}$ $=48 \mathrm{~N}$ <br> tension $>$ friction hence particle starts to move | B1 <br> E1 | 2 |  |
| (d) | when particle is next at rest, work done against friction is EPE at B $13.6 \times$ distance $=28.8$ <br> distance is 2.1176 $=2.12 \mathrm{~m}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 2 | CAO |
| (e) | total distance is $5+2.1176$ $=7.12 \mathrm{~m}$ | B1 | 1 | ft from M1 in (d) <br> or total distance $\times 13.6=$ original EPE, $96.8$ <br> total distance is 7.12 m |
|  | Total |  | 14 |  |

(Q8, Jan 2012)

| 31 (a) | $\begin{aligned} \text { KE } & =\frac{1}{2} \times 76 \times 28^{2} \\ & =29792 \mathrm{~J} \\ & =29800 \mathrm{~J} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 | All terms correct |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $\text { Change in PE: } \begin{aligned} m g h & =76 \times 9.8 \times 31 \mathrm{~J} \\ & =23088.8 \mathrm{~J} \\ & =23100 \mathrm{~J} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 2 | All terms correct |
| (c)(i) | KE when touches down on ground $\begin{aligned} & =29792+23088.8 \mathrm{~J} \\ & =52881 \mathrm{~J} \\ & =52900 \mathrm{~J} \end{aligned}$ | M1 <br> A1 | 2 | Their values, one correct CAO |
| (ii) | $\begin{aligned} & \text { Speed of Alan is } \sqrt{\frac{52881}{\frac{1}{2} \times 76}} \\ & =37.304 \mathrm{~m} \mathrm{~s}^{-1} \\ & =37.3 \mathrm{~m} \mathrm{~s}^{-1} \end{aligned}$ | M1 <br> A1 | 2 | CAO |
|  | Total |  | 8 |  |

\begin{tabular}{|c|c|c|c|c|}
\hline 32 (a) \& \begin{tabular}{l}
\[
\begin{aligned}
\text { Initial EPE } \& =\frac{\lambda x^{2}}{2 l} \\
\& =\frac{120 \times(0.5)^{2}}{2 \times 5} \\
\& =3 \mathrm{~J}
\end{aligned}
\] \\
Initial KE is \(\frac{1}{2} \times 0.4 \times 9^{2}=16.2 \mathrm{~J}\) \\
When block is at \(A, \frac{1}{2} m v^{2}=3+16.2\)
\[
v^{2}=19.2 \div 0.2=96
\] \\
Speed is \(9.80 \mathrm{~m} \mathrm{~s}^{-1}\)
\end{tabular} \& M1
A1

M1

A1 \& 4 \& M1 for formula with extension 0.5
Accept $4 \sqrt{6}$; condone 9.79 <br>

\hline (b)(i) \& | Normal reaction is $m g=0.4 g$ Frictional force is $0.4 \mu \mathrm{~g} \mathrm{~N}$ |
| :--- |
| Work done by frictional force is $5.5 \times(0.4 \mu g)$ or $2.2 \mu g$ | \& | M1 |
| :--- |
| A1 |
| m1 | \& \& <br>

\hline \& C of Energy, when at $A$, gives

$$
\begin{aligned}
& 19.2-5.5 \times(0.4 \mu g)=\frac{1}{2} \times 0.4 \times v^{2} \\
& 19.2-2.2 \mu g=0.2 v^{2} \\
& v=\sqrt{96-11 \mu g}
\end{aligned}
$$ \& M1

A1

A1 \& 6 \& | Three terms, eg initial energy in (a) ( $=3$ or 19.2); work done; KE at $A$. |
| :--- |
| Fully correct |
| Ft $v=\sqrt{\left(v^{2} \text { in }(\mathrm{a})\right)-11 \mu g}$ | <br>

\hline (ii) \& | Speed when rebounding is $\frac{1}{2} \sqrt{96-11 \mu g}$ |
| :--- |
| Block is stationary at $B$ $\begin{aligned} & \frac{1}{2} \times 0.4 \times \frac{1}{4}(96-11 \mu g)-2.2 \mu g \\ & =\frac{120 \times(0.5)^{2}}{2 \times 5} \\ & \frac{1}{2} \times 0.1(96-11 \mu g)-2.2 \mu g=3 \\ & 4.8-2.75 \mu g=3 \\ & \mu=0.0668 \end{aligned}$ | \& | B1ft |
| :--- |
| M1 |
| A1 |
| A1 |
| A1 |
| A1 | \& 6 \& Three terms Two terms correct with sign Third term correct with sign Or $4.8-0.55 \mu g-2.2 \mu g=3$ <br>

\hline \& Total \& \& 16 \& <br>
\hline
\end{tabular}

(Q8, June 2012)

| 33 (a) | $\begin{aligned} \mathrm{KE} & =\frac{1}{2} \times 0.16 \times 11^{2} \\ & =9.68 \mathrm{~J} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 |  |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $\text { Change in PE: } \begin{aligned} m g h & =0.16 \times 9.8 \times 5 \\ & =7.84 \mathrm{~J} \end{aligned}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 2 |  |
| (c)(i) | KE when reached point $B$ $\begin{aligned} & =9.68-7.84 \mathrm{~J} \\ & =1.84 \mathrm{~J} \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 | $\begin{aligned} & \text { '(a)' }-{ }^{\prime}(\mathbf{b})^{\prime} \\ & \text { cao } \end{aligned}$ |
| (ii) | Speed of ball is $\sqrt{\frac{1.84}{\frac{1}{2} \times 0.16}}$ | M1 |  | If added in (c)(i) 0 marks for (c)(i) 14.8 M1A1for $\mathbf{c}(\mathbf{i i})$ |
|  | $\begin{aligned} & =4.7958 \mathrm{~m} \mathrm{~s}^{-1} \\ & =4.80 \mathrm{~m} \mathrm{~s}^{-1} \end{aligned}$ | A1 | 2 | Condone 4.8,4.79 |
|  | Total |  | 8 |  |

(Q1, Jan 2013)

| 34 | Force acting against gravity is $m g \sin \theta$ Force acting against gravity and resistance is $m g \sin \theta+8000$ $\begin{aligned} & =1500 \times g \times \sin \theta+8000 \\ & =8588 \mathrm{~N} \text { or } 8590 \mathrm{~N} \end{aligned}$ $\begin{aligned} \text { Using power } & =\text { force } \times \text { velocity } \\ & =8588 \times 22 \\ & =188936 \mathrm{~W} \\ & =189 \mathrm{~kW} \end{aligned}$ | M1 <br> A1 <br> M1 <br> dep <br> A1 <br> A1 | 5 | Condone $\cos \theta$ or -1 for M marks <br> Accept 188.9 or 188 |
| :---: | :---: | :---: | :---: | :---: |
|  | Total |  | 5 |  |

(Q3, Jan 2013)

\begin{tabular}{|c|c|c|c|c|}
\hline 35 (a) \& \[
\begin{aligned}
\text { Work done } \& =\int_{0}^{e} \frac{\lambda x}{l} \mathrm{~d} x \\
\& =\left[\frac{\lambda x^{2}}{2 l}\right]_{0}^{e} \\
\& =\frac{\lambda e^{2}}{2 l}
\end{aligned}
\] \& M1
A1
A1 \& 3 \& \(\mathrm{SC} 1 \int_{0}^{e} \frac{\lambda e}{l} d e\) SC1 \(\int \frac{\lambda x}{l} d x\) with no limits \\
\hline (b)(i) \& \begin{tabular}{l}
\(\operatorname{Using} T=\frac{\lambda x}{l}:\)
\[
\begin{aligned}
5 g \& =\frac{392 x}{1.6} \\
x \& =\frac{5 g \times 1.6}{392} \\
\& =0.2
\end{aligned}
\] \\
Extension is 0.2 m
\end{tabular} \& M1

A1 \& 2 \& <br>
\hline (ii) \& When extension is

\[
$$
\begin{aligned}
0.6 \mathrm{~m}, & \text { EPE }=\frac{\lambda x^{2}}{2 l} \\
= & \frac{392 \times(0.6)^{2}}{2 \times 1.6} \\
= & 44.1 \mathrm{~J}
\end{aligned}
$$

\] \& | B1 |
| :--- |
| M1 |
| A1 | \& 3 \& B1 for 0.6 <br>


\hline (iii) \& | Let $y$ metres be distance particle is above A. |
| :--- |
| C of energy, when particle has speed $0.8 \mathrm{~m} \mathrm{~s}^{-1}$, gives $\begin{aligned} & 5 \times g \times y+\frac{392 \times(0.6-y)^{2}}{2 \times 1.6}+\frac{1}{2} \times 5 \times 0.8^{2} \\ & =\frac{392 \times(0.6)^{2}}{2 \times 1.6} \end{aligned}$ | \& M1A1

A1F \& \& M1 4 terms, 2 correct M1A1 4 terms, 3 correct M1A2 4 terms correct Ft answer to (b)(ii) <br>

\hline \& $$
\begin{aligned}
& 49 y+122.5(0.6-y)^{2}+1.6=122.5 \times 0.6^{2} \\
& 49 y-147 y+122.5 y^{2}+1.6=0 \\
& 122.5 y^{2}-98 y+1.6=0 \\
& y=\frac{98 \pm \sqrt{98^{2}-4 \times 122.5 \times 1.6}}{2 \times 122.5} \\
& y=\frac{98 \pm 93.9148}{245} \\
& \quad=0.016674 \text { and } 0.7833
\end{aligned}
$$ \& A1 \& \& if $x$ used instead of $0.6-y$, A1 here for $x=0.5833 \ldots$ <br>

\hline \& \& E1 \& 5 \& <br>
\hline \& Total \& \& 13 \& <br>
\hline
\end{tabular}


(Q2, June 2013)

| 37 | $\begin{aligned} & \text { Using power }=\text { force } \times \text { velocity } \\ & 240000=F \times 20 \\ & F=12000 \\ & \text { Accelerating force is } 12000-5000 \\ & \text { Using } F=7000 \mathrm{~N} \\ & 22000 a=7000 \\ & a=0.318 \text { or } \frac{7}{22} \mathrm{~m} \mathrm{~s}^{-2} \end{aligned}$ | M1A1 <br> A1 <br> B1 <br> M1 <br> A1 | 6 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Total |  |  |  |



